

(23)

Arithmetic Sequence

An arithmetic sequence is a sequence that forms a pattern by the same nonzero number by adding or subtracting.

An arithmetic sequence forms a linear function b/c of the constant rate of change or common difference.

$$a_n = a_1 + (n-1)(d)$$

D: common difference

N: term we are finding

a_1 : 1st Term

Ex) 9, 13, 17, 21, ..., 25, 29, 33

$\begin{matrix} \vee & \vee & \vee & & & & \\ +4 & +4 & +4 & & & & \\ & & & d=4 & & & \end{matrix}$

Ex) $-\frac{3}{4}, -\frac{1}{4}, \frac{1}{4}, \frac{3}{4}, \dots, \frac{5}{4}, \frac{7}{4}, \frac{9}{4}$

$d = \frac{1}{4}$

Ex) The 25th term; $a_1 = 5$, $d = -2$

$$a_{25} = 5 + (25-1)(-2)$$

$$a_{25} = -53$$

Ex) Find the 16th term: 4, 8, 12, 16, ...

$$\begin{array}{ccc} \vee & \vee & \vee \\ +4 & +4 & +4 \end{array}$$

$$d = 4$$

$$n = 16$$

$$a_1 = 4$$

$$a_{16} = 4 + (16-1)(4)$$

$$a_{16} = 64$$

Ex) Find the 60th term: 11, 5, -1, -7, ...

$$\begin{array}{ccc} \vee & \vee & \vee \\ -6 & -6 & -6 \end{array}$$

$$d = -6$$

$$n = 60$$

$$a_1 = 11$$

$$a_{60} = 11 + (60-1)(-6)$$

$$a_{60} = -343$$

Ex) Find the "nth" term: 13, 23, 33, 43, ...

$$\begin{array}{ccc} \vee & \vee & \vee \\ +10 & +10 & +10 \end{array}$$

$$d = 10$$

$$n = n$$

$$a_1 = 13$$

$$a_n = 13 + (n-1)(10)$$

$$= 13 + 10n - 10$$

$$a_n = 3 + 10n$$

Ex) Find the "nth" term: -31, -34, -37, -40, ...

$$\begin{array}{ccc} \vee & \vee & \vee \\ -3 & -3 & -3 \end{array}$$

$$d = -3$$

$$n = n$$

$$a_1 = -31$$

$$a_n = -31 + (n-1)(-3)$$

$$= -31 - 3n + 3$$

$$a_n = -3n - 28$$